

# **PATENT**

#### IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

IN RE THE PATENT APPLICATION OF: Bellaiche, L., et al.

Appl. No.: 10/632,740 Group Art Unit: 1755

Filed: 08/01/2003 Examiner: Koslow, C.

For: Enhanced Electromechanical Properties in Atomically-Ordered Ferroelectric Alloys

Mail Stop Amendment Commissioner for Patents P.O. Box 1450 Alexandria, VA 22313-1450

### **DECLARATION UNDER RULE 131**

- 1. This declaration is to establish completion of the invention in this application in the United States, at a date prior to December 2001, that is the effective date of the prior art publication (the Thesis by A. George) that was cited by the examiner in the office action of August 31, 2004.
  - 2. The persons making this declaration are the inventors.

## Facts and Documentary Evidence

3. To establish the date of completion of the invention of this application, the following attached documents are submitted as evidence:

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4. The examiner's attention is particularly directed to the last full paragraph on page 56 of the document cited above. This paragraph is quoted in its entirety as follows:

"We also numerically found (results not shown here) that continuously increasing v from 0 to 0.44 leads to a continuous decrease of the orthorhombic-to-monoclinic transition temperature from 373 K to 0 K. As a result, the temperature at which  $d_{34}$  and  $\chi_{33}$  both peak depends on the value of the v parameter. This dependency could lead to the development of devices with electromechanical performances optimized for any temperature between 373 K and 0 K."

This paragraph also appears at paragraph [0018] of the specification.

- 5. Laurent Bellaiche had been studying the effects of atomic ordering in various ferroelectric alloys at the University of Arkansas in May 2000 when he suggested a project to Aaron George as the basis for a Master's Thesis. Bellaiche had previously published a study along with R. Hemphill which examined rocksalt ordering. George developed computer code to generate orderings besides rocksalt in particular directions. Bellaiche and George investigated various orderings using disordered alloys with rocksalt as the reference point.
- 6. By August 2000, the analyses by Bellaiche and George suggested different orderings that produced an increase in electromechanical responses and gave insights into the effect of polarization rotation in the crystals.
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used an inverse method of generating orderings producing large responses. A four plane period was agreed upon as an experimentally feasible and interesting possibility to explore.

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I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that the statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section

1001 of Title 18 of the United States Code, and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

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Attorney Docket No. 8793-52026

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# Anomalous properties in ferroelectrics induced by atomic ordering

A. M. George, Jorge Íñiguez & L. Bellaiche

Physics Department, University of Arkansas, Fayetteville, Arkansas 72701, USA

Complex insulating perovskite alloys are of considerable technological interest because of their large dielectric and piezoelectric responses. Examples of such alloys include (Ba<sub>1-x</sub>Sr<sub>x</sub>)TiO<sub>3</sub>, which has emerged as a leading candidate dielectric material for the memory-cell capacitors in dynamic random access memories1; and Pb(Zr<sub>1-x</sub>Ti<sub>x</sub>)O<sub>3</sub> (PZT), which is widely used in transducers and actuators2. The rich variety of structural phases that these alloys can exhibit, and the challenge of relating their anomalous properties to the microscopic structure, make them attractive from a fundamental point of view. Theoretical investigations of modifications to the atomic ordering of these alloys suggest the existence of further unexpected structural properties3 and hold promise for the development of new functional materials with improved electromechanical properties. Here we report ab initio calculations that show that a certain class of atomic rearrangement should lead simultaneously to large electromechanical responses and to unusual structural phases in a given class of perovskite alloys. Our simulations also reveal the microscopic mechanism responsible for these anomalies.

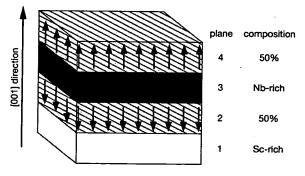
The class of Pb(Mg<sub>1/3</sub>Nb<sub>2/3</sub>)O<sub>3</sub>-PbTiO<sub>3</sub> (PMN-PT) and Pb(Zn<sub>1/3</sub>Nb<sub>2/3</sub>)O<sub>3</sub>-PbTiO<sub>3</sub> (PZN-PT) perovskite ferroelectric alloys have been reported4 to show remarkably large piezoelectric constants around 2,000 pC N<sup>-1</sup>. These materials thus promise improvements in the resolution and range of ultrasonic and sonar listening devices<sup>5</sup>. Perovskite A(B'B"...)O<sub>3</sub> alloys are also of great interest, as demonstrated by the discovery of an unexpected monoclinic phase<sup>6</sup> in Pb(Zr<sub>1-x</sub>Ti<sub>x</sub>)O<sub>3</sub>. These two findings have led to a search for materials with even larger electromechanical response and/or currently unobserved phases. In particular, if a mechanism can be found that occurs in a large number of ferroelectric alloys, markedly enhances the piezoelectricity and the dielectric responses, and leads to unexpected structural features, that mechanism is likely to have large technological and fundamental implications. Here we report that such a mechanism exists and simply consists in rearranging in a certain way the atoms in a heterovalent alloy (that is, an alloy made of atoms belonging to different columns of the periodic table). More precisely, we predict that materials made of the sequences  $Pb(Sc_{0.5+}^{3+}, Nb_{0.5-+}^{5+})O_3/$  $Pb(Sc_{0.5}^{3+}Nb_{0.5}^{5+})O_3/Pb(Sc_{0.5-}^{3+}Nb_{0.5+}^{5+})O_3/Pb(Sc_{0.5}^{3+}Nb_{0.5}^{5+})O_3$  along the [001] direction should show very large electromechanical responses,

and unusual monoclinic and orthorhombic phases for some values of the  $\nu$  parameter. The analysis of our results points to the different valence of the B atoms (Sc and Nb) as the main reason for the existence of these anomalous properties.

Here, we use the numerical scheme proposed in refs 7 and 8, which consists of constructing an effective hamiltonian for the alloy from first-principles calculations, to predict the properties of  $Pb(Sc_{1-x}Nb_x)O_3$  (PSN) structures. This effective hamiltonian<sup>7,8</sup> contains a local-mode self-energy (expanded in even-order terms up to fourth order of the phonon local soft modes), a long-range dipole–dipole interaction, a short-range interaction between soft modes (quadratic order of the soft modes), an elastic energy (expanded to second order of the strain variables), and an interaction between the local modes and local strain (second order of the soft modes and first order in strain). It also contains an energy term describing the effects of the atomic configuration on the phonon local soft modes (which are directly related to the electrical polarization) which can be written as

$$\Delta E = -\sum_{i} Z^* \mathbf{u}_{i} \cdot \left[ \sum_{j} - \sigma_{j} S_{ji} \hat{\mathbf{e}}_{ji} \right]$$
 (1)

where i runs over all the cells and j runs over the three nearestneighbour shells of cell i. Here  $\mathbf{u}_i$  is the local soft mode in cell i,  $Z^*$  is the Born effective charge associated with the local soft modes, and  $\hat{\mathbf{e}}_{ii}$ is the unit vector joining the B site j to the B site i. The variables  $\{\sigma_i\}$ characterize the atomic configuration:  $\sigma_i = +1$  (-1) indicates that there is an Nb (Sc) ion in cell j.  $S_{ji}$  is an alloy-related parameter that only depends on the distance between the B sites i and j, and is derived from first-principles calculations9-12 on small cells. Equation (1) indicates that  $\Delta E$  can be viewed as the interaction energy between the dipole moment  $Z^*\mathbf{u}_i$  associated with the site i and an internal electric field  $\Sigma_j - \sigma_j S_{ji} \hat{\mathbf{e}}_{ji}$  induced by the B ions of sites j on the site i. Moreover, we numerically find that the  $S_{ii}$ parameters all have negative signs. As a result, the radial electric field  $-\sigma_i S_{ii} \hat{\mathbf{e}}_{ii}$  acting on site *i* and induced by a  $Sc^{3+}$  (Nb<sup>5+</sup>) ion sitting on site j is directed from the site i to the site j (respectively, from site j to site i). This is consistent with an electrostatic picture of PSN since Sc (Nb) ions are negatively (positively) charged with respect to the average B-ion valence of 4+. The effective hamiltonian approach yields good agreement with direct first-principles results in PZT and PSN alloys 7.8. Previous works (see refs 7-8) have found that a linear rescaling of the simulation temperature often leads to good agreement with experiment. Adopting this approach again here, our temperatures are rescaled down by a factor of 2.5 so that the theoretical Curie temperature in disordered PSN is forced to match the experimental value<sup>13</sup>. The need for such rescaling may be due to higher perturbative terms or the rotation of the oxygen

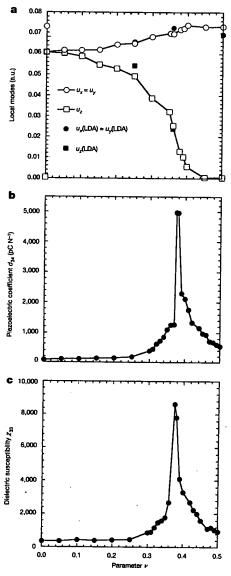


**Figure 1** Schematic representation of the ferroelectric structures considered here. The materials are  $Pb(SC_{0.5+}^{3+},Nb_{0.5-}^{5+},)O_3/Pb(SC_{0.5}^{3+}Nb_{0.5}^{5+})O_3/Pb(SC_{0.5}^{3+}Nb_{0.5+}^{5+})O_3/Pb(SC_{0.5}^{3+}Nb_{0.5+}^{5+})O_3$  structures. The internal electric fields acting on the four B planes are indicated by arrows.

octahedra, neglected in our effective model of PSN.

Here, we use the total energy of our alloy effective hamiltonian in Monte Carlo simulations to calculate finite-temperature properties of some selected Pb( $Sc_{1-x}Nb_x$ )O<sub>3</sub> structures. We consider structures with the following sequence of four B-planes along the [001] direction (Fig. 1): a niobium-poor plane for which  $x = 0.5 - \nu$ , a second plane made of 50% scandium and 50% niobium (x = 0.5), a niobium-rich plane with  $x = 0.5 + \nu$ , and a fourth plane similar to the second one. The B atoms are randomly distributed within each of these four planes. The studied structures only differ in the value of the parameter  $\nu$ , which is allowed to vary from zero (in the case of the disordered PSN alloy) to 0.5 (in the case in which the first plane is entirely made of Sc atoms and the third plane is fully occupied by Nb atoms). We use  $12 \times 12 \times 12$  supercells, implying that the sequence of the four different B(001) planes is repeated three times, to get well converged results<sup>7,8</sup>.

Figure 2a shows the cartesian coordinates  $(u_x, u_y \text{ and } u_z)$ —along



**Figure 2** Properties of the studied structures as a function of the  $\nu$  parameter at 20 K. a, Average cartesian coordinates  $u_x$ ,  $u_y$  and  $u_z$  of the local mode; b, the  $d_{34}$  piezoelectric coefficient; c, the  $\chi_{33}$  dielectric susceptibility. The filled symbols in a represent the cartesian coordinates  $u_x$ (LDA),  $u_y$ (LDA) and  $u_z$ (LDA) of the local modes predicted by direct first-principles calculations made using the local density approximation  $^{9-12}$ . a.u., arbitrary units.

# letters to nature

the [100], [010] and [001] directions, respectively—of the supercell average of the local mode vectors as a function of this parameter  $\nu$  at 20 K. The structure for which  $\nu$  is null has  $u_x = u_y = u_z \neq 0$ . This characterizes a ferroelectric rhombohedral structure in which the polarization is directed along the pseudo-cubic [111] direction, consistent with experiments on disordered PSN samples<sup>13</sup>. Interestingly, increasing  $\nu$  results in a strong decrease of  $u_z$  whereas  $u_x$  and u, slowly increase and remain equal to each other. This behaviour corresponds to a ferroelectric phase of monoclinic symmetry for which the polarization lies between the [111] and [110] directions (the one denoted M<sub>B</sub> in ref. 14). When  $\nu$  is larger than 0.44,  $u_z$ becomes null and  $u_x$  and  $u_y$  reach their maximum value, indicating that the resulting phase is now of orthorhombic symmetry with a polarization lying along the [110] direction. Increasing the parameter  $\nu$  thus leads to three different ground states and to a continuous rotation of the electrical polarization. To our knowledge, the predicted monoclinic M<sub>B</sub> ground state has never been observed in any perovskite material without the aid of external stress

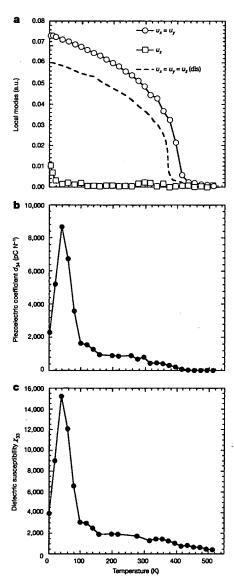


Figure 3 Properties of the structure associated with  $\nu=0.375$  as a function of temperature. Panels  ${\bf a}$ ,  ${\bf b}$  and  ${\bf c}$  display the same property as the corresponding panels of Fig. 2. Dashed line in a shows one of the three cartesian coordinates  $(u_x)$  of the local mode in disordered (dis) PSN (the two other cartesian coordinates are nearly identical to the one displayed, and are omitted for clarity).

or electric field. Similarly, we are not aware of any studies pointing to an orthorhombic ground state in PSN. The existence of these monoclinic and orthorhombic phases is due to the energy term described in equation (1). Figure 2a also shows the predictions of local density approximation<sup>9-11</sup> calculations performed on 20-atom supercells mimicking the structures corresponding to  $\nu = 0.25$ ,  $\nu = 0.36$  and  $\nu = 0.50$ . In these supercells, each B(001) plane is represented by a virtual atom corresponding to the composition in this plane<sup>12,15</sup>. The direct first-principles calculations agree with the predictions of our effective hamiltonian approach, thus further supporting the existence of these unusual monoclinic and orthorhombic phases.

Figure 2b summarizes the effects of the parameter  $\nu$  on piezo-electricity and Fig. 2c the effects on dielectric response at 20 K. We found that the electromechanical coefficients most affected by the atomic ordering are the shear  $d_{34}$  piezoelectric coefficient and the  $\chi_{33}$  dielectric susceptibility, when expressing both piezoelectric and dielectric tensors in the orthonormal basis formed by  $a_1 = [100]$ ,  $a_2 = [010]$  and  $a_3 = [001]$ . More precisely, Fig. 2b shows that  $d_{34}$  reaches a peak and remains at large values for a broad range of  $\nu$  centred around the monoclinic-to-orthorhombic phase transition. Figure 2c demonstrates that the studied atomic ordering simultaneously results in a large dielectric response, as  $\chi_{33}$  achieves values above 1,000 at 20 K when  $\nu$  is greater than 0.3.

We now investigate the finite-temperature properties of a structure showing one of the largest electromechanical responses at 20 K. More precisely, we focus on the structure for which  $\nu = 0.375$ . Figure 3a shows the cartesian coordinates of the supercell average of the local mode vectors as a function of temperature for this structure, and compares them with those of the disordered PSN material. Each coordinate of the local mode in each structure is close to zero at high temperature, characterizing a paraelectric phase. At a temperature close to 373 K, the disordered material undergoes a transition from a paraelectric cubic phase to a ferroelectric rhombohedral structure (for which  $u_x = u_y = u_z$ ), consistent with experiments<sup>13</sup>. The disordered PSN material then remains in the rhombohedral phase for lower temperature. On the other hand, the modulated structure with  $\nu = 0.375$  adopts three different phases: a paraelectric tetragonal phase induced by atomic ordering (for which  $u_x = u_y = u_z = 0$ ) at high temperature, an orthorhombic ferroelectric phase  $(u_x = u_y \neq 0 \text{ and } u_z = 0)$  for temperature between 400 K and 40 K, and the monoclinic ferroelectric M<sub>B</sub> phase  $(u_x = u_y > u_z)$ , with  $u_z \neq 0$  for temperature lower than 40 K. As shown in Fig. 3b and c, the existence of the orthorhombic-tomonoclinic phase transition results in huge electromechanical responses peaking around this transition and occurring over a broad range of temperature. In fact,  $d_{34}$  and  $\chi_{33}$  are greater than  $1,500 \, pC \, N^{-1}$  and 3,000, respectively, for any temperature lower than 100 K.

We also numerically found (results not shown here) that continuously increasing  $\nu$  from 0 to 0.44 leads to a continuous decrease of the orthorhombic-to-monoclinic transition temperature from 373 K to 0 K. As a result, the temperature at which  $d_{34}$  and  $\chi_{33}$  both peak depends on the value of the  $\nu$  parameter. This dependency could lead to the development of devices with electromechanical performances optimized for any temperature between 373 K and 0 K.

The intriguing results of Figs 2 and 3 can be understood by means of equation (1). The internal electric field  $\Sigma_j - \sigma_j S_{ji} \hat{e}_{ji}$  acting on each B(001) plane is represented in Fig. 1. The atoms in plane 2 feel an internal electric field oriented along the  $[00\bar{1}]$  direction whereas the atoms in plane 4 feel an internal electric field along the [001] direction. It is straightforward to demonstrate that the magnitude of these fields is linearly dependent on the parameter  $\nu$ . (These features can be understood qualitatively by simple short-range electrostatic considerations: the difference of valence between Sc and Nb atoms leads to charged B(001) planes with ionic charges

linearly dependent on v. When electrostatic interactions up to the third-neighbour shells are included, these charged planes generate internal electric fields whose directions are those of Fig. 1 and whose magnitudes are linearly dependent on  $\nu$ .) Increasing  $\nu$  thus results in stronger internal fields with opposite directions. These strong opposite fields tend to suppress the polarization's component along the direction of compositional modulation. As a result,  $u_z$ becomes smaller than  $u_x$  and  $u_y$ . The studied structures with intermediate values of v thus first undergo a paraelectric-toorthorhombic ferroelectric transition at high temperature before adopting the monoclinic  $M_B$  phase for ground state. The modulated structures with the largest values of  $\nu$  have the strongest internal electric fields, which annihilate  $u_z$  at any temperature. Consequently, such structures never reach the monoclinic phase and instead adopt the orthorhombic phase for ground state. The large values of  $d_{34}$  and  $\chi_{33}$  shown in Figs 2 and 3 simply reflect the considerable change of uz when some parameters are slightly modified ( $\nu$  at a fixed temperature, or T for a fixed value of  $\nu$ ), especially for structures at the borderline between the monoclinic and orthorhombic phases. In other words, the large electromechanical responses are consistent with the ease of rotating the polarization<sup>7,16</sup>. We have shown here results for the thinnest possible structures. For larger structures, with thicker layers, the 'unusual' electromechanical responses will be smaller due to smaller internal electric fields.

On the basis of the electrostatic considerations discussed above, we expect that any alloy made of heterovalent atoms and with a rhombohedral ground state in its disordered form should have the structural, piezoelectric and dielectric anomalies displayed in Figs 2 and 3, when the atomic ordering along the [001] direction is adjusted in a certain way. The atomically ordered structures discussed here could be grown by means of a pulse laser deposition technique<sup>17</sup> or by using molecular beam epitaxy.

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- Abe, K. & Komatsu, S. Ferroelectric properties in epitaxially grown Ba<sub>x</sub>Sr<sub>1-x</sub>TiO<sub>3</sub> thin films. J. Appl. Phys. 77, 6461–6465 (1995).
- 2. Uchino, K. Piezoelectric Actuators and Ultrasonic Motors (Kluwer Academic, Boston, 1996).
- Sai, N., Meyer, B. & Vanderbilt, D. Compositional inversion symmetry breaking in ferroelectric perovskites. Phys. Rev. Lett. 84, 5636-5639 (2000).
- Park, S.-E. & Shrout, T. R. Ultrahigh strain and piezoelectric behavior in relaxor based ferroelectric single crystal. J. Appl. Phys. 82, 1804–1811 (1997).
- 5. Service, R. F. Shape-changing crystals get shiftier. Science 275, 1878 (1997).
- Noheda, B. et al. A monoclinic ferroelectric phase in the Pb(Zr<sub>1-x</sub>Ti<sub>x</sub>)O<sub>3</sub> solid solution. Appl. Phys. Lett. 74, 2059–2061 (1999).
- Bellaiche, L., García, A. & Vanderbilt, D. Finite-temperature properties of Pb(Zr<sub>1-x</sub>Ti<sub>x</sub>)O<sub>3</sub> alloys from first principles. Phys. Rev. Lett. 84, 5427-5430 (2000).
- Hemphill, R., Bellaiche, L., García, A. & Vanderbilt, D. Finite-temperature properties of disordered and ordered Pb(Sc<sub>0.5</sub>Nb<sub>0.5</sub>)O<sub>3</sub> alloys. Appl. Phys. Lett. 77, 3642–3644 (2000).
- 9.4 Hohenberg, P. & Kohn, W. Inhomogeneous electron gas. Phys. Rev. 136, B864-871 (1964).
- Kohn, W. & Sham, L. J. Self-consistent equations including exchange and correlation effects. Phys. Rev. 140, A1133-1138 (1965).
- Vanderbilt, D. Soft self-consistent pseudopotentials in a generalized eigenvalue formalism. Phys. Rev. B 41, 7892–7895 (1990).
- Bellaiche, L. & Vanderbilt, D. Virtual crystal approximation revisited: Application to dielectric and piezoelectric properties of perovskites. Phys. Rev. B 61, 7877-7882 (2000).
- Chu, F., Reaney, I. M. & Setter, N. Spontaneous (zero-field) relaxor-to-ferroelectric-phase transition in disordered Pb(Sc<sub>12</sub>Nb<sub>12</sub>)O<sub>3</sub>. J. Appl. Phys. 77, 1671–1676 (1995).
- Vanderbilt, D. & Cohen, M. H. Monoclinic and triclinic phases in higher-order Devonshire theory. — Phys. Rev. B 63, 094108 (2001).
- Ramer, N. J. & Rappe, A. M. Application of a new virtual crystal approach for the study of disordered perovskites. J. Phys. Chem. Solids 61, 315

  –320 (2000).
- Fu, H. & Cohen, R. E. Polarization rotation mechanism for ultrahigh electromechanical response in single crystal piezoelectrics. Nature 403, 281–283 (2000).
- Brazier, M., McElfresh, M. & Mansour, S. Unconventional hysteresis behavior in compositionally graded F6(Zr,Ti)O<sub>3</sub> thin films. Appl. Phys. Lett. 72, 1121–1123 (1998).

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